

The Solid State



Semi crystalline Crystalline Amorphous short range order only Long range order

"For most crystallographers it is long-range order that sets crystals apart from glasses and amorphous solids. But condensed-matter physicists have recognized that there is a structural continuum between ideal crystals and amorphous solids.". Gautam Desiraju : Nature 2013

### Interaction of X-ray radiation with solids

- Collision of the X-ray photon with a charged particle causes the component of the particle to oscillate with the same frequency.
- The oscillating particle returns to the resting state by emitting a photon that travels outward.

#### The Math

Debye's Equation describes the interaction of radiation between two identical "atoms" i and jseparated by the distance  $r_{ii}$ 

- $I(s) = \sum_{i=1}^{2} \sum_{j=1}^{2} f_i(s) f_j(s) \frac{\sin 2\pi s r_{ij}}{2\pi s r_{ij}}$
- Where  $s = 2 \sin \theta / \lambda$  and  $f(s) = \sum a e^{-bs^2} + c$ *a*, *b*, *c* are the Cromer–Mann coefficients for a given element

For a diatomic molecule of the same element the maxima for Debye's equation will be ~  $r_{ij}s_m =$ given s =  $2 \sin \theta / \lambda$  then :

$$K\lambda = 2r_m \sin\theta_m K = 1.23$$

# Wide Angle Scattering (WAXS) (Powder Diffraction) How do we do **Data Collection**

Debye's Equation  $[I(s) = \sum_{i=1}^{N} \sum_{j=1}^{N} f_i(s) f_j(s) \frac{\sin 2\pi s r_{ij}}{2\pi s r_{ij}}]$  describes the **Amorphous WAXS** in general terms.

> For a VERY simple system (all orientations are present) where the average contact distances are near 1.5, 2.5 and 5 Å we can predict the scattered pattern given below. ( $\lambda$ =1.54Å). Intensity decreases (exponentially) as 20 increases



For a linear ordered system where the same element (atom) is spaced at equal distance(s) of a > 2 times then

 $I(s) = \left[ f e^{2\pi i s r} + f e^{2\pi i s (r+a)} + \cdots f e^{2\pi i s (r+Na)} \right]^2 \left[ \frac{\sin N 2\pi a s}{N 2\pi a s} \right]^2$ 

**I**(2*θ*)

given: 
$$\left[\frac{\sin N2\pi as}{N2\pi as}\right]^2 \sim \frac{1}{N^2} \left[\frac{\sin N2\pi as}{\sin 2\pi as}\right]^2$$
 the

$$I(s) \sim f^2 \left[ \frac{\sin N2\pi as}{\sin 2\pi as} \right]$$

**2***θ* 

As *N* increases the peak sharpens until N>1000 atoms at which time you reach the line width of the instrument.

	For a 3D ordered system (Crystalline)
	$F(s) = \sum_{1}^{N} f_n(s) e^{2\pi i s r}$ $r = xa + yb + zc$ (unit cell as vectors)
<b>,</b>	$F(s) = \sum_{1}^{N} f_n(s) e^{2\pi i s (xa+yb+zc)}  \text{Given } s \cdot a = h, s \cdot b = k, s \cdot c = l$
	$F(s) = \sum_{1}^{N} f_n(s) e^{2\pi i (hx + ky + lz)} \text{ and } I(s) \approx  F(s) ^2$
	For the 3D ordered systems $I(s)$ will have maxima at discrete positions
1.23	$hx + ky + lz \implies 2\theta_{hkl}$ $2\theta_{hkl} = 2 \times \sin^{-1}((a^{*2}h^2 + b^{*2}k^2 + c^{*2}l^2 + 2b^*c^*kl\cos\alpha^* + 2a^*c^*hl\cos\beta^* + 2a^*b^*hk\cos\gamma^*)^{1/2}/2)$
	h=2,k=1,l=2
=1, <i>k</i> =1, <i>l</i>	$I=0$ $I(2,1,2) \approx F(2,1,2)^2$ [atoms (e <sup>-</sup> ) in 2,1,2 plane]
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## **stalline**

- $a = h, s \cdot b = k, s \cdot c = l$
- $\approx |F(s)|^2$

## axima at discrete positions



BRAGG BRENTANO : The detector is positioned at  $2\theta$  angle to collect the data. The number of X-rays counted by the detector is proportional to the intensity (I) of the scattered X-ray



Qualitative Analysis





X-rays diverge from the source (A) strike the specimen (B) and



Transmission with Area detection. The area (2D) detector is positioned behind the sample. X-rays travel; through the sample and are collected at the detector

 Re
 I
 Be
 N
 S
 P
 I
 Es

 186.2
 9.012
 14.01
 32.06
 90.977
 126.9
 252